

Quiz IV

This is a 50 minute closed-book exam; no notes. Please put your name on the top sheet. Answer all three questions. Explain your working and state any assumptions you have made.

1 (3 points) Circle the correct answer.

1. The design equation for double-pipe heat exchangers

- is independent of the area of the heat exchanger.
- involves the log-mean temperature difference.
- is used in the (ϵ, NTU) method.
- has a correction factor $F = 0.5$.
- comes from solving the Navier–Stokes equations.

2. The overall heat transfer coefficient U

- only depends on conduction.
- is not used in double-pipe heat exchangers.
- is always determined by experiment.
- is obtained by adding in series convective and conductive resistances.
- is independent of Prandtl number.

3. Heat exchanger effectiveness ϵ

- is the same as taking $F = 1$.
- cannot be used to find tube pass lengths.
- only applies to laminar flows.
- involves the maximum possible heat transfer in the denominator.
- is independent of T_h at the hot inlet.

2 (7 points) Water ($C_p = 1 \text{ kJ/kg}\cdot\text{K}$) at 80°C flows through a cross-flow exchanger of area 10 m^2 at a rate of 900 kg/h . Cooling water at 15°C is available. If the water flow rate is 450 kg/h , find the exit temperatures. Take $U = 200 \text{ W/m}^2\cdot\text{K}$.

$$C_H = \dot{m} \cdot c_p = 900 \text{ (kg/h)} \times \frac{1}{3600} \text{ (h/sec)} \times 1000 \text{ (J/kg}\cdot\text{K)} = 250 \text{ (J/s}\cdot\text{K)}$$

$$C_C = \dot{m} \cdot c_p = 450 \text{ (kg/h)} \times \frac{1}{3600} \text{ (h/sec)} \times 1000 \text{ (J/kg}\cdot\text{K)} = 125 \text{ (J/s}\cdot\text{K)} \Rightarrow C_{\min}$$

$$NTU = \frac{UA}{C_{\min}} = \frac{200 \times 10}{125} = 16 \text{ (off chart)} \Rightarrow \epsilon_c \approx 0.9$$

$$\begin{aligned} \epsilon_c &= \frac{T_{c2} - T_{c1}}{T_{H1} - T_{c1}} = 0.9 \Rightarrow T_{c2} = 0.9(T_{H1} - T_{c1}) + T_{c1} \\ &= 0.9(80 - 15) + 15 = 73.5 \text{ (}^\circ\text{C)} \end{aligned}$$

$$\begin{aligned} C_C(T_{c2} - T_{c1}) &= C_H(T_{H1} - T_{H2}) \Rightarrow T_{H2} = T_{H1} - \frac{C_C}{C_H}(T_{c2} - T_{c1}) \\ &= 80 - 0.5(73.5 - 15) = 56.25 \text{ (}^\circ\text{C)} \end{aligned}$$

3 (10 points) Show that for a cylindrical pipe of conductivity k with inner and outer radii r_1, r_2 , the overall heat transfer coefficient U based on the outer area is

$$U = \left[\frac{1}{h_2} + \frac{r_2}{k} \ln(r_2/r_1) + \frac{r_2}{r_1} \frac{1}{h_1} \right]^{-1},$$

where h_1 and h_2 are the heat transfer coefficients at the inner and outer surfaces.

Carbon tetrachloride (boiling point at 1 atm: 76.7°C ; heat capacity on a molar basis: $c_p = 131.3 \text{ J/mol}\cdot\text{K}$; atomic weights of carbon and chlorine 12 and 35.45 g/mol respectively) is cooled from its boiling point as it flows through a cocurrent heat double-pipe heat exchanger. The pipe is made of stainless steel ($k = 16 \text{ W/m}\cdot\text{K}$) with inner and outer diameters 1.2 and 1.3 cm respectively. Water ($C_p = 1 \text{ kJ/kg}\cdot\text{K}$) at a flow rate of 200 kg/s enters at 25°C and leaves at 40°C . The heat transfer coefficients of the inner and outer surfaces are both $800 \text{ W/m}^2\cdot\text{K}$ and the length of the pipe is 4 m . Calculate the flow rate of carbon tetrachloride and its outlet temperature.

$$Q = 2\pi L \frac{T_i - T_o}{\frac{1}{r_2 h_2} + \frac{\ln(r_2/r_1)}{k} + \frac{1}{r_1 h_1}} = U A \Delta T$$

$$A = A_2 = 2\pi r_2 L$$

(Above)

$$\frac{2\pi L (T_i - T_o)}{\frac{1}{r_2 h_2} + \frac{\ln(r_2/r_1)}{k} + \frac{1}{r_1 h_1}} = 2\pi r_2 L U_o (T_i - T_o)$$

U_o : the overall heat transfer coefficient

$$\Rightarrow U_o = \left[\frac{1}{h_2} + \frac{r_2 \ln(r_2/r_1)}{k} + \frac{r_2}{r_1} \frac{1}{h_1} \right]^{-1}$$

$$Q = (\dot{m} \cdot c_p)_c (T_{c2} - T_{c1}) = U_o A \Delta T_{lm}$$

$$i) (\dot{m} \cdot c_p)_c (T_{c2} - T_{c1}) = (200 \times 10^3) (40 - 25) = 3 \times 10^6 \text{ (W)}$$

$$ii) U_o A \Delta T_{lm} = \left[\frac{1}{h_2} + \frac{r_2}{k} \ln(r_2/r_1) + \frac{r_2}{r_1} \frac{1}{h_1} \right]^{-1} \cdot (2\pi r_2 L) \cdot \frac{T_{H2} - T_{c2} - (T_{H1} - T_{c1})}{\ln\left(\frac{T_{H2} - T_{c2}}{T_{H1} - T_{c1}}\right)}$$

$$= \left[\frac{1}{800} + \frac{0.0065}{16} \ln\left(\frac{0.0065}{0.006}\right) + \frac{0.0065}{0.006} \cdot \frac{1}{800} \right]^{-1} (2\pi \times 0.0065 \times 4) \cdot \frac{(T_{H2} - 40) - (16.7 - 25)}{\ln\left(\frac{T_{H2} - 40}{16.7 - 25}\right)}$$

$$= 61.95 \cdot \frac{T_{H2} - 16.7}{\ln\left(\frac{T_{H2} - 40}{51.7}\right)}$$

$$\frac{T_{H2} - 16.7}{\ln\left(\frac{T_{H2} - 40}{51.7}\right)} = \frac{3 \times 10^6}{61.95} = 48426 \Rightarrow T_{H2}$$

$$(\dot{m} \cdot c_p)_c (T_{c2} - T_{c1}) = (\dot{m} \cdot c_p)_H (T_{H2} - T_{H1}) \Rightarrow \text{get } (\dot{m} \cdot c_p)_H$$

$$(c_p)_H = 0.854 \text{ (kJ/kg}\cdot\text{K)}$$

$$\Rightarrow \dot{m}_H$$

