

Quiz IV

This is a 50 minute closed-book exam. Please put your name on the top sheet. Answer all three questions. Explain your working and state any assumptions you have made.

1 (3 points) Circle the correct answer.

1. For a perfect gas, entropy

- remains a constant.
- is a function of pressure, temperature and electric field.
- is a thermodynamic function of state.
- depends only on the area of a nozzle.
- decreases through shocks.

2. The Mach number

- depends on the state via temperature alone for an ideal gas.
- is constant in space for a given flow.
- is all that is needed to compute the state of the fluid.
- depends only on the area of a nozzle.
- is never 1 in a converging-diverging nozzle.

3. Isentropic flow in a duct

- only has shocks at locations with maximum area.
- corresponds to vertical lines on a T - s diagram.
- has constant pressure.
- has increasing velocity as the duct area decreases in all cases.
- is always supersonic.

2 (7 points) The stagnation pressure in a Mach 2 wind tunnel operating with air is 900 kPa. A sphere of diameter 1 cm positioned in the wind tunnel has a drag coefficient of 0.95. Calculate the drag force on the sphere.

3 (10 points) A converging-diverging nozzle discharges air at supersonic speeds. The flow has velocity $V_1 = 150 \text{ ms}^{-1}$, pressure $p_1 = 100 \text{ kPa}$ and temperature $T_1 = 20^\circ\text{C}$ at section 1 upstream of the throat. The area at the throat is 0.1 m^2 . Compute the mass flow rate.

Useful values and parameters

Units and constants

1 hp = 550 lb ft/s

1 in = 2.54 cm

1 mile = 1609 m

1 mph = 88 ft/min

Acceleration of gravity: $g = 9.81$, $g = 32.2$ ft/s²

$^{\circ}\text{R} = ^{\circ}\text{F} + 459.67$

Material properties (SI unless otherwise stated)

Air: $\rho = 1.23$ and $\mu = 1.79 \times 10^{-5}$ at 15°C

Air: $\rho = 2.38 \times 10^{-3}$ slugs/ft³ and $\mu = 3.47 \times 10^{-7}$ lb·s/ft³ at 59°F

Air (ideal gas): $c_p = 1004$, $R = 287.1$ (SI), $R = 1,716.5$ ft lb/slug °R (BG), $R = 53.35$ ft lb/lbm °R (EE)

Isentropic flow of an ideal gas with $k = 1.4$

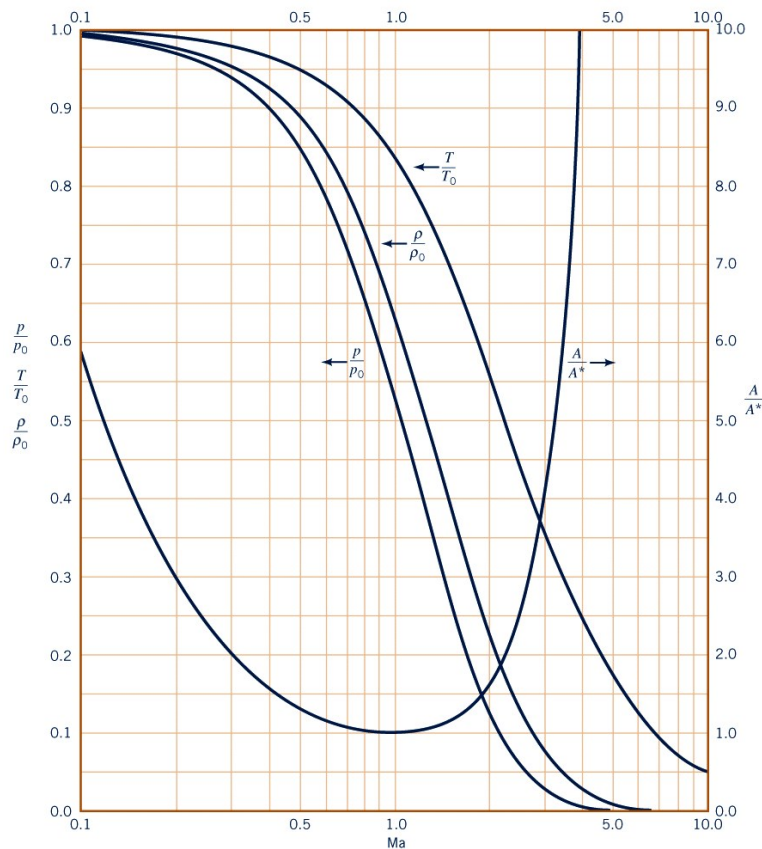


Figure D.1
Graph provided by Dr. Bruce A. Reichert