

From Entropy to Networks

The Future of Communication Engineering Through the Lens of Network Information Theory

Young-Han Kim

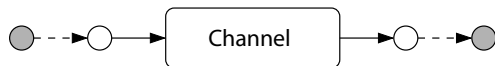
University of California, San Diego

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Chinese University of Hong Kong

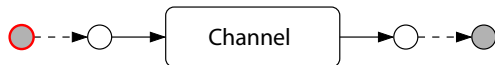
July 19, 2013

Joint work with Fatemeh Arbabjolfaei (UCSD), Bernd Bandemer (UCSD), Sae-Young Chung (KAIST), Abbas El Gamal (Stanford), Sung Hoon Lim (Samsung), Eren Şaşoğlu (Berkeley), Lele Wang (UCSD)

Point-to-point communication

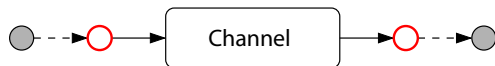


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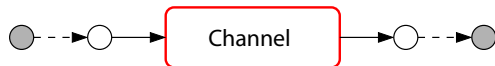
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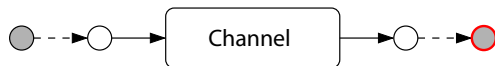
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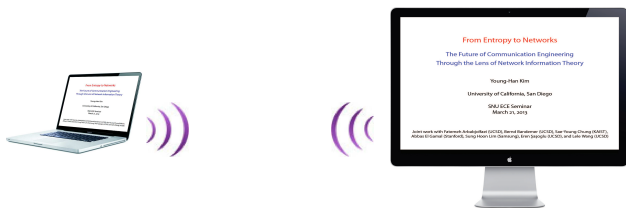
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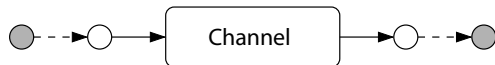
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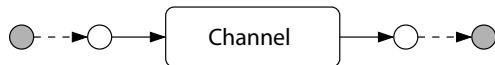
Information flow questions



Question 1

What is the **limit on communication** (how much/how fast)?

Information flow questions



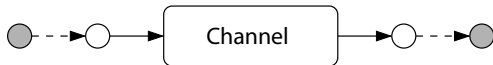
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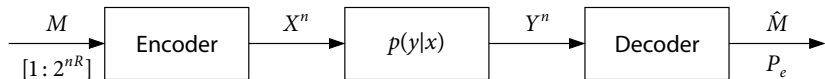
Question 2

What are the **coding schemes/techniques** that achieve this limit?

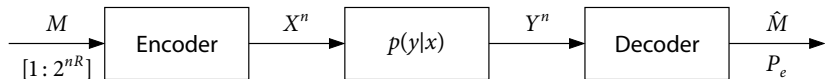
Answer 1: Channel coding theorem



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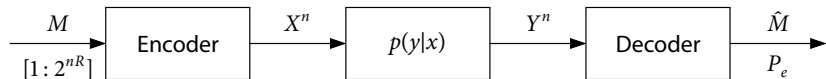


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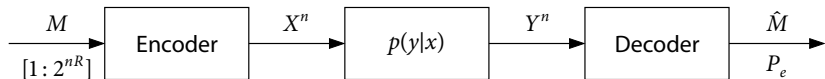
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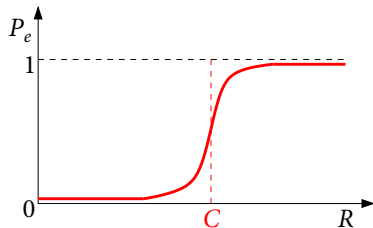


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- Capacity C : maximum R such that $P_e \rightarrow 0$ as $n \rightarrow \infty$

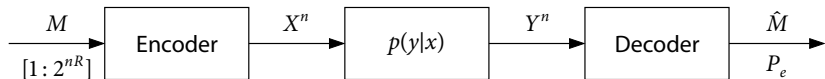
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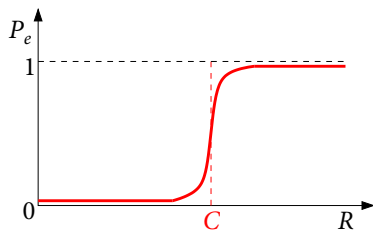
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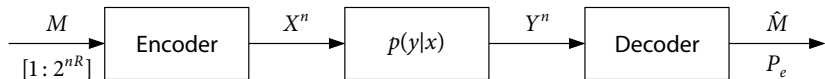
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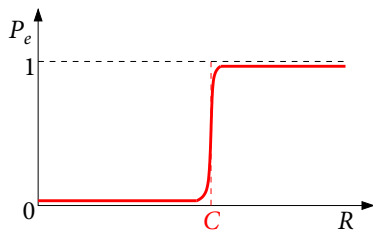
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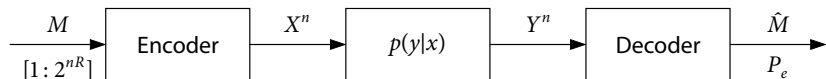
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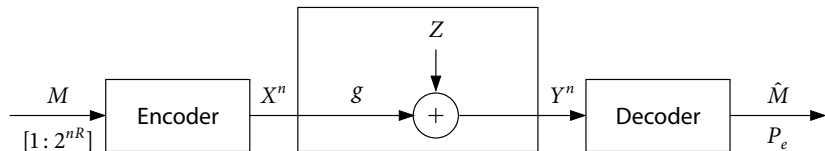


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Shannon (1948)

$$C = \max_{p(x)} I(X; Y)$$

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Shannon (1948)

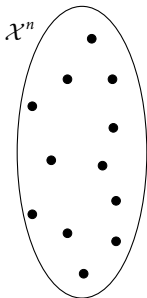
$$C = \frac{1}{2} \log(1 + S) = C(S)$$

Answer 2: Proof of achievability

- Random coding and joint typicality decoding
(Shannon 1948, Forney 1972, Cover 1975a)

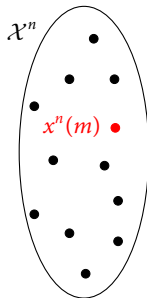
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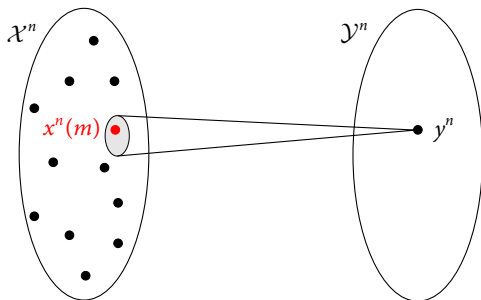
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 - ▶ “All codes are good, **except those that we know of**”
(Wozencraft–Reiffen 1961, Forney 1995)

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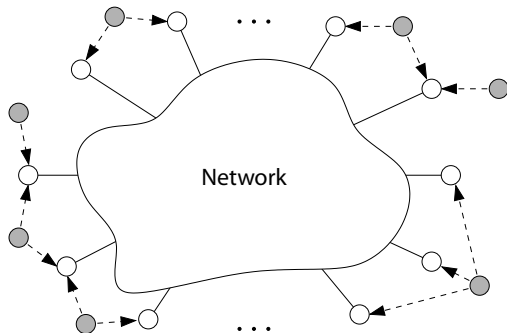
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- Algebraic/combinatorial/probabilistic coding theory
 - ▶ Hamming, Reed–Solomon, BCH, LDPC, turbo, raptor, polar, spatially coupled codes
 - ▶ 0.0045 dB of the Shannon limit (Chung–Forney–Richardson–Urbanke 2001)

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- IEEE CTW 2010 panel discussion: is communication theory dead?

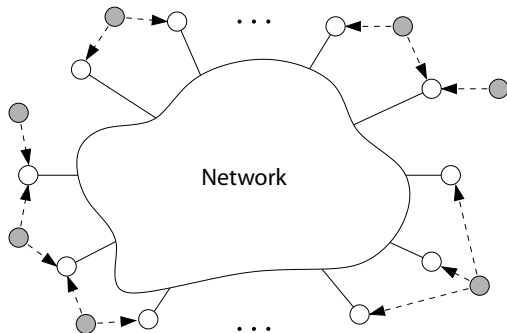


Networked information processing system



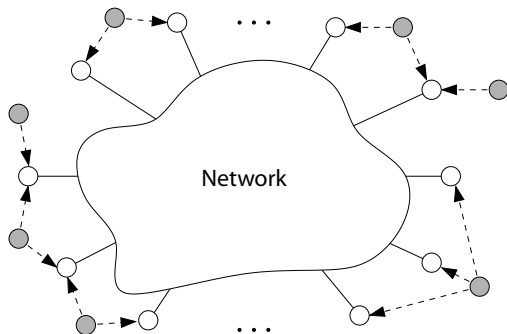
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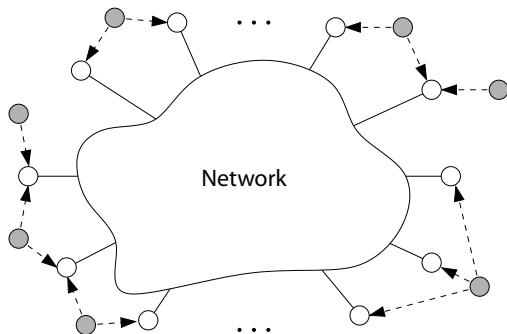
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- **Task:** Communicate sources or make decision based on them

Network information flow questions



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- What are the **coding schemes/protocols/architectures** that achieve this limit?

Network information theory

- **Multiple** sources and destinations

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Network information theory

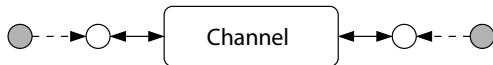
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Network information flow questions

- Network capacity
- Optimal coding schemes/protocols/architectures

Brief history

- First paper (Shannon 1961): “two-way communication channels”

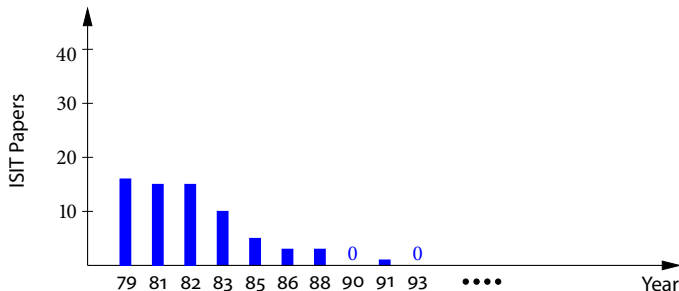


Brief history

- First paper (Shannon 1961): “two-way communication channels”
- Significant research activities in 70s and early 80s
 - 😊 Broadcast, multiple access, interference, and relay channels
 - 😊 Distributed compression and multiple description coding

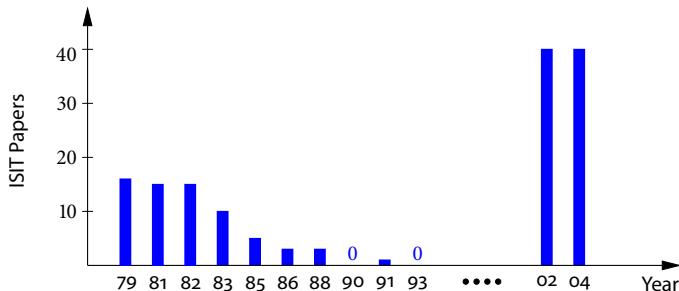
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 - ☺ Broadcast, multiple access, interference, and relay channels
 - ☺ Distributed compression and multiple description coding
 - ☹ Many basic problems open
 - ☹ Little interest from practice



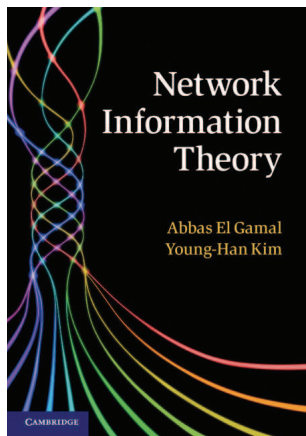
Brief history

- First paper (Shannon 1961): “two-way communication channels”
- Significant research activities in 70s and early 80s
- **Wireless** communications and the **Internet** revived interest in mid 90s
 - ▶ Some progress on old open problems and many new problems
 - ▶ Very large number of papers in ISIT, T-IT, T-COM, T-WC, ...
 - ▶ Results starting to have an impact on real-world networks



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- State of the theory: El Gamal–K (2011)



Outline of the talk

- Canonical problems in network communication

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 - ▶ Multiple unicast
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- **Solutions** from network information theory

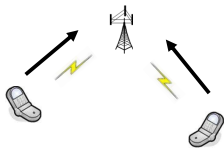
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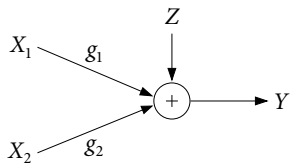
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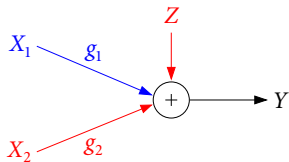
Multiple access (uplink) communication



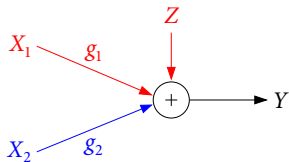
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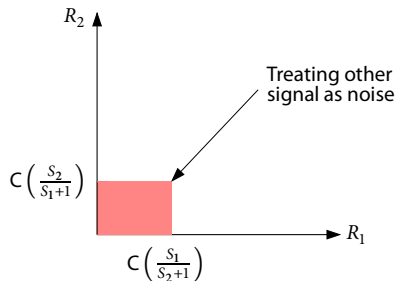
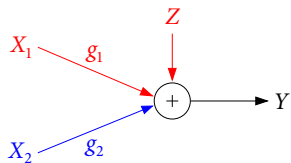
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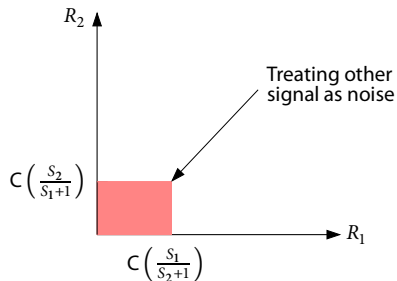
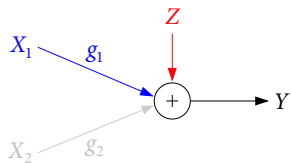
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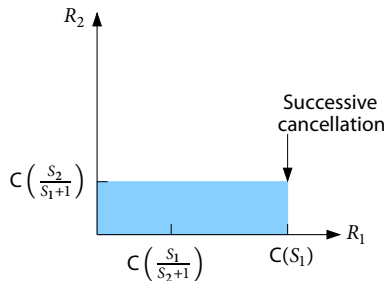
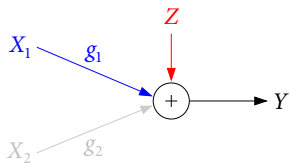
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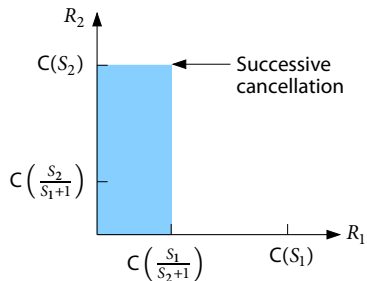
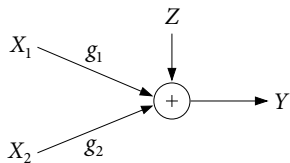
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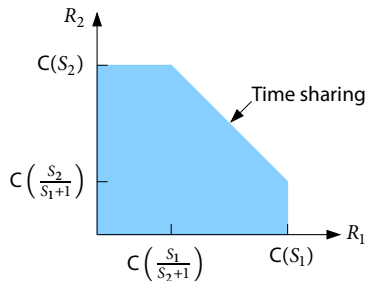
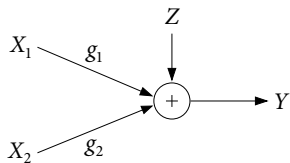
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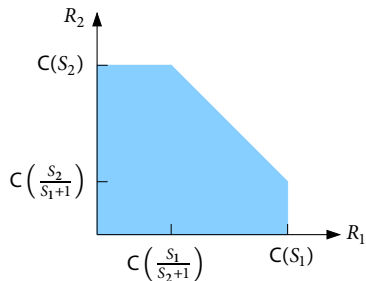
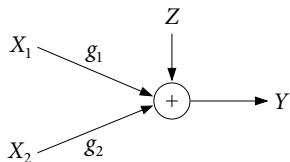
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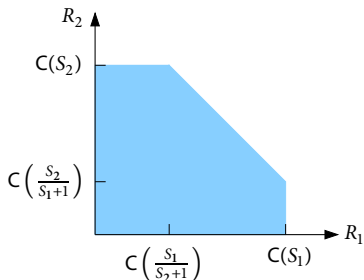
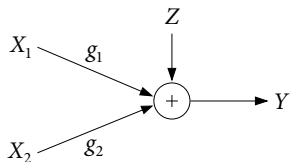


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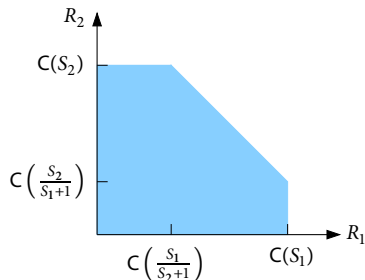
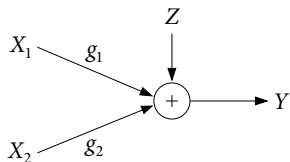
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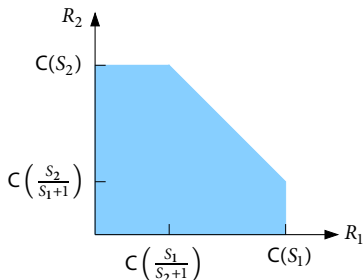
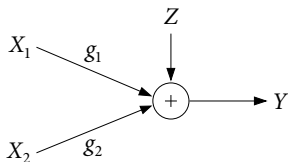
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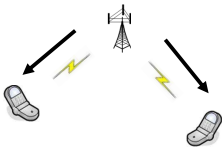
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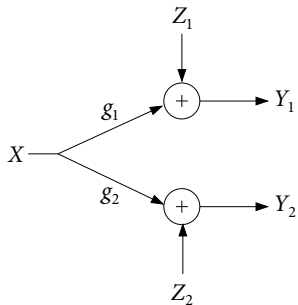


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- **Good point-to-point codes + signal processing suffices!**

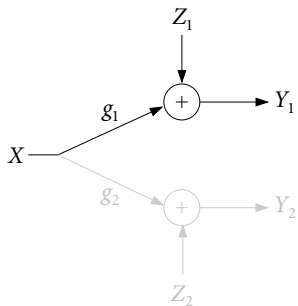
Broadcast (downlink) communication



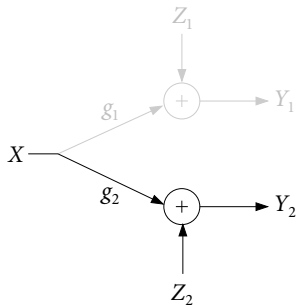
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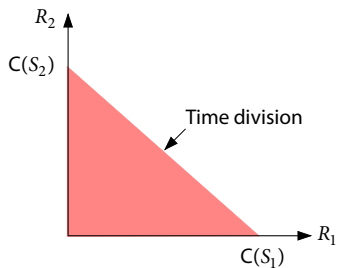
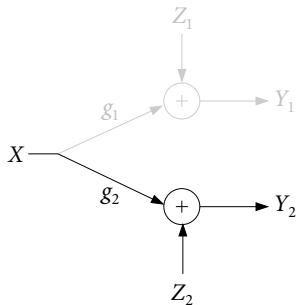
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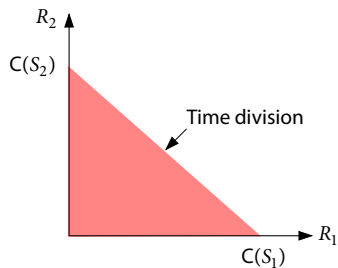
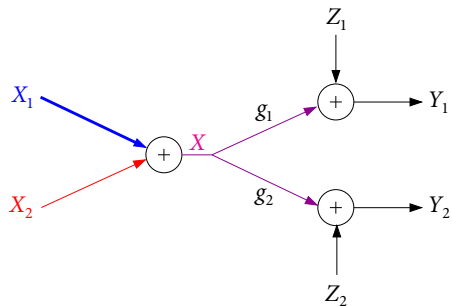
Broadcast (downlink) communication



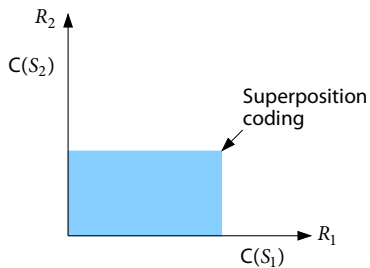
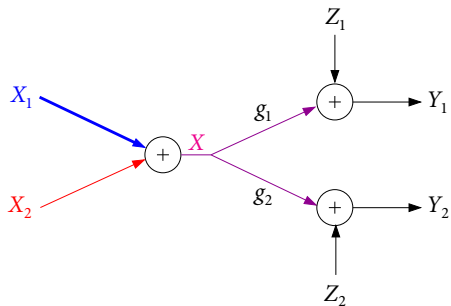
Broadcast (downlink) communication



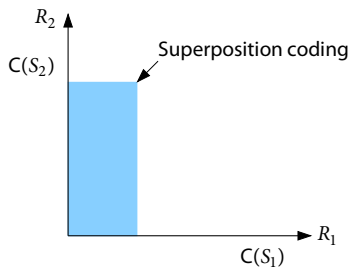
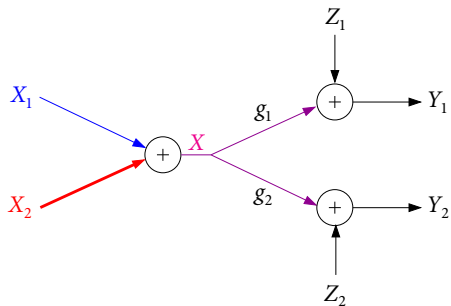
Broadcast (downlink) communication



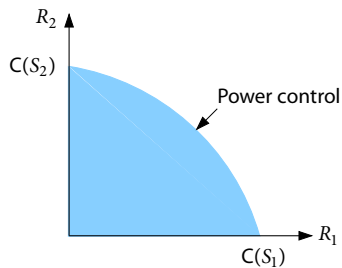
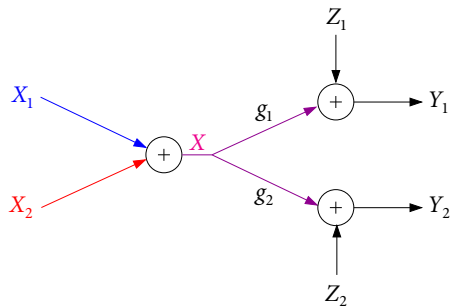
Broadcast (downlink) communication



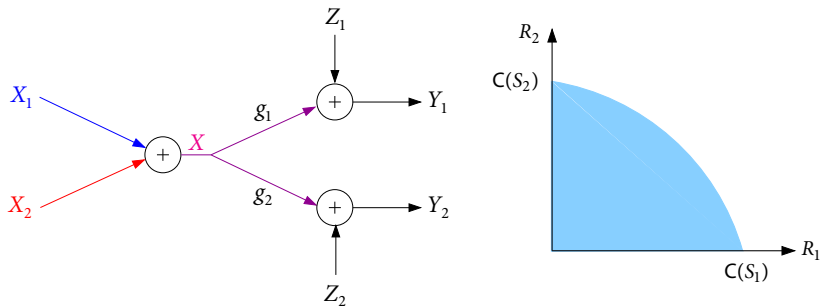
Broadcast (downlink) communication



Broadcast (downlink) communication

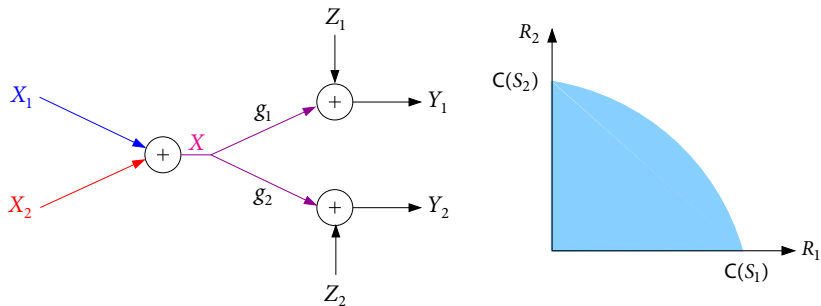


Broadcast (downlink) communication



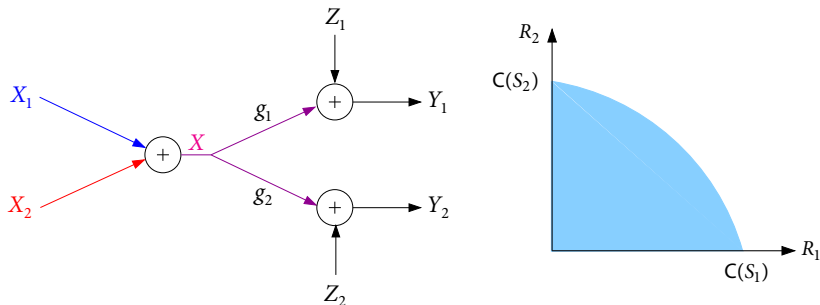
- Optimal (Cover 1972, Bergmans 1973, 1974, Gallager 1974)

Broadcast (downlink) communication



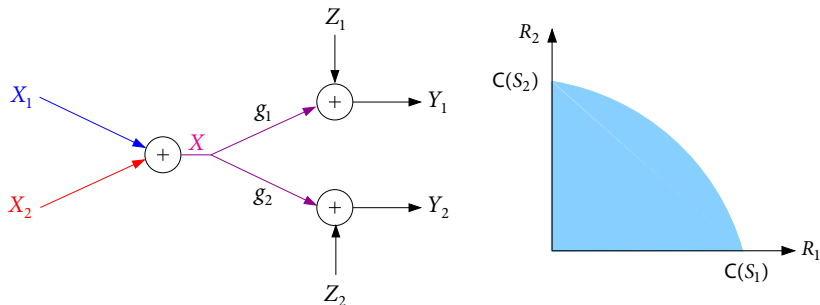
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- Hierarchical modulation: DVB-T, 3GPP2 UMB

Broadcast (downlink) communication



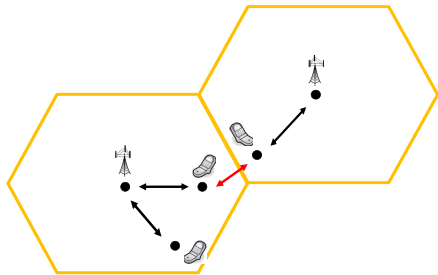
- Optimal (Cover 1972, Bergmans 1973, 1974, Gallager 1974)
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- Can be generalized to any number of single-antenna receivers

Broadcast (downlink) communication

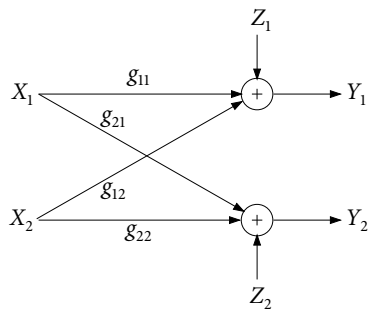


- Optimal (Cover 1972, Bergmans 1973, 1974, Gallager 1974)
- Hierarchical modulation: DVB-T, 3GPP2 UMB
- Can be generalized to any number of single-antenna receivers
- **Good point-to-point codes + signal processing suffices!**

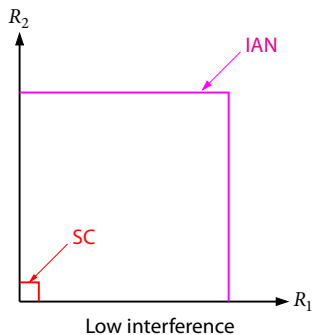
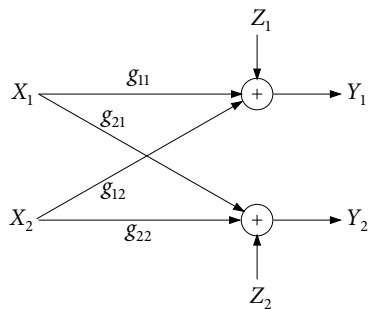
Interference (multicell) communication



Interference (multicell) communication

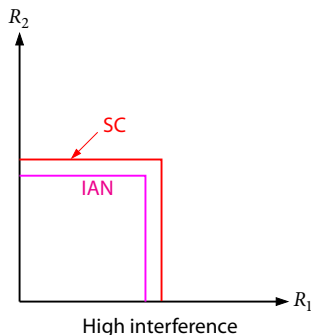
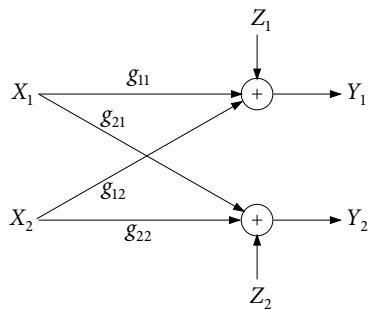


Interference (multicell) communication



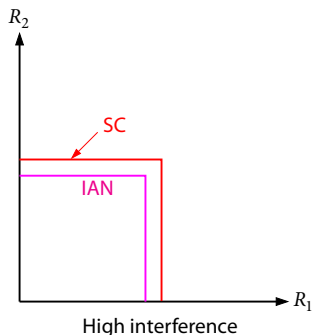
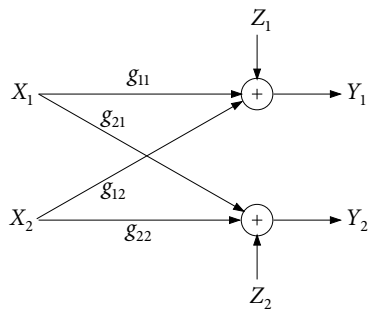
- Low interference: **treating interference as noise (IAN)** performs well
- High interference: **successive cancellation (SC)** performs well

Interference (multicell) communication



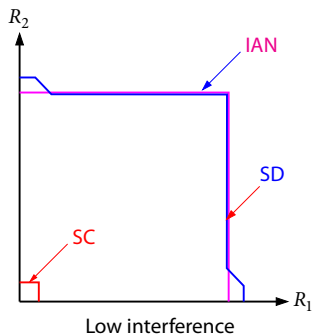
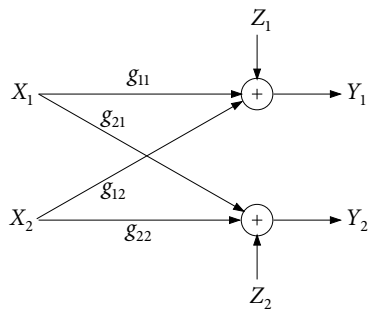
- Low interference: **treating interference as noise (IAN)** performs well
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- Neither is optimal in general; nor is **time division**

Interference (multicell) communication



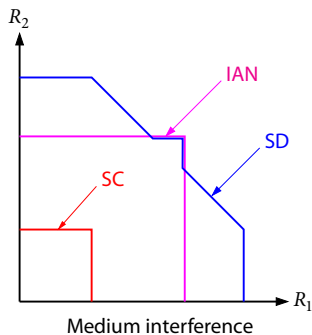
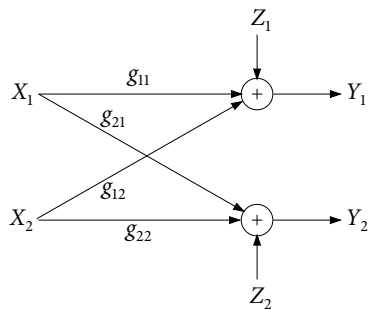
- Low interference: **treating interference as noise (IAN)** performs well
- High interference: **successive cancellation (SC)** performs well
- Neither is optimal in general; nor is **time division**
- In general, we need more than **good point-to-point codes + signal processing**

Interference (multicell) communication



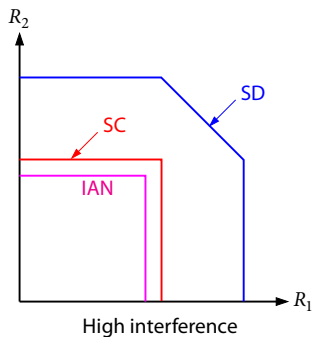
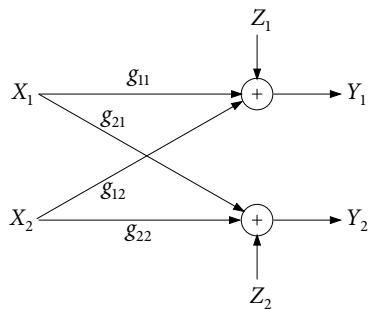
- Simultaneous decoding

Interference (multicell) communication



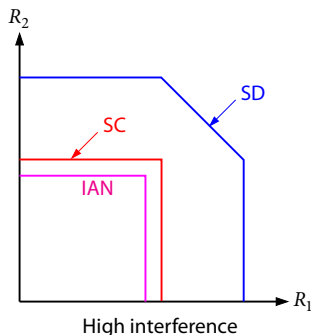
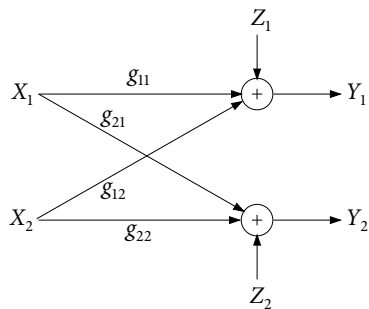
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Interference (multicell) communication



- Simultaneous decoding

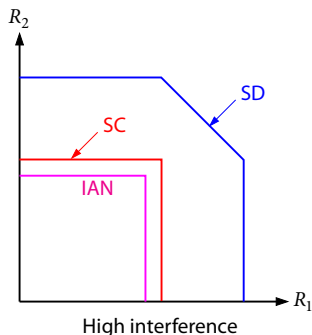
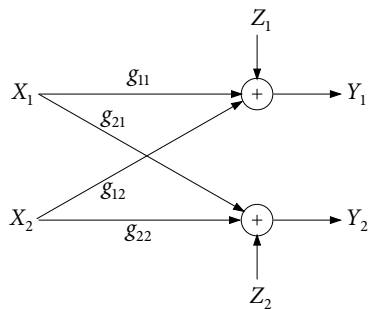
Interference (multicell) communication



- Simultaneous decoding

- ▶ Always better than **treating interference as noise** and **successive cancellation**

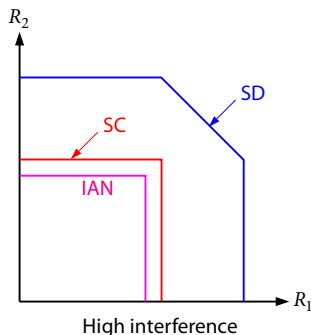
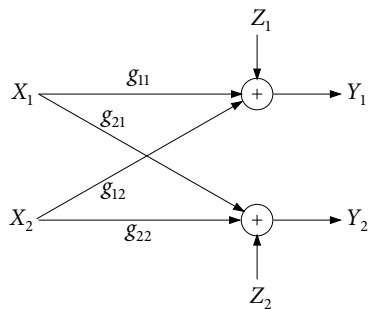
Interference (multicell) communication



- Simultaneous decoding

- ▶ Always better than **treating interference as noise** and **successive cancellation**
- ▶ Optimal under random coding (Bandemer–El Gamal–K 2012)

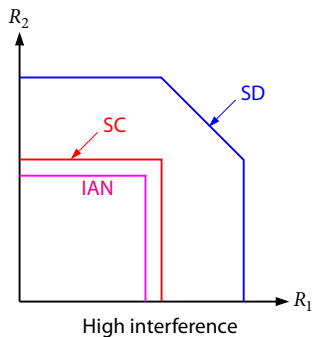
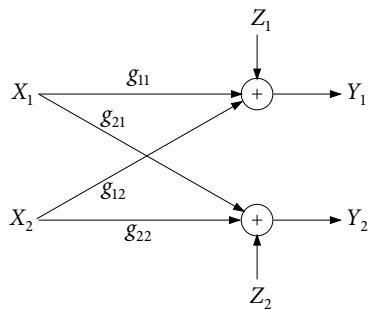
Interference (multicell) communication



- Simultaneous decoding

- ▶ Always better than **treating interference as noise** and **successive cancellation**
- ▶ Optimal under random coding (Bandemer–El Gamal–K 2012)
- ▶ + **superposition coding**: optimal within 1/2 bit (Etkin–Tse–Wang 2008)

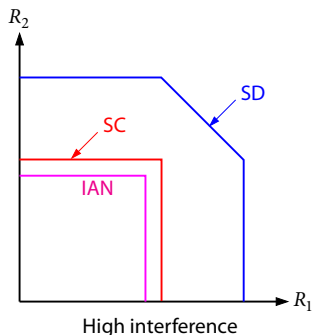
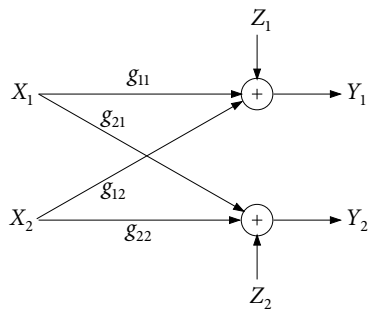
Interference (multicell) communication



Conclusion 1

Interference-aware coding schemes can boost performance tremendously

Interference (multicell) communication



Conclusion 1

Interference-aware coding schemes can boost performance tremendously

Challenge 1

Low-complexity implementation of simultaneous decoding

More on simultaneous decoding

- **Maximum likelihood decoding (MLD):** At receiver 1, find

$$\begin{aligned} & \arg \max_{\hat{m}_1} f(y_1^n | x_1^n(\hat{m}_1)) \\ &= \arg \max_{\hat{m}_1} \sum_{m_2} f(y_1^n | x_1^n(\hat{m}_1), x_2^n(m_2)) \\ &= \arg \max_{\hat{m}_1} \sum_{m_2} \exp(-\|y_1^n - g_{11}x_1^n(\hat{m}_1) - g_{12}x_2^n(m_2)\|^2/2) \end{aligned}$$

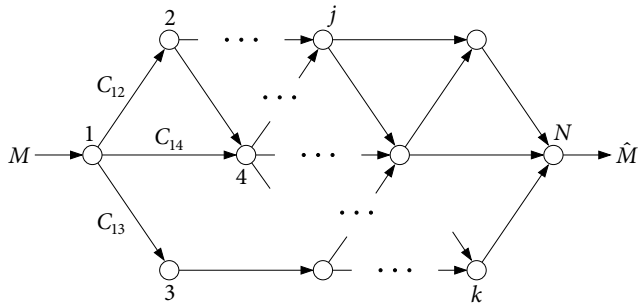
- Simultaneous decoding (Bandemer–El Gamal–K 2012):

$$\begin{aligned} & \approx \arg \max_{\hat{m}_1} \max_{m_2} \exp(-\|y_1^n - g_{11}x_1^n(\hat{m}_1) - g_{12}x_2^n(m_2)\|^2/2) \\ &= \arg \max_{\hat{m}_1} \max_{m_2} -\|y_1^n - g_{11}x_1^n(\hat{m}_1) - g_{12}x_2^n(m_2)\| \\ &= \arg \min_{\hat{m}_1} \min_{m_2} \|y_1^n - g_{11}x_1^n(\hat{m}_1) - g_{12}x_2^n(m_2)\| \end{aligned}$$

Outline of the talk

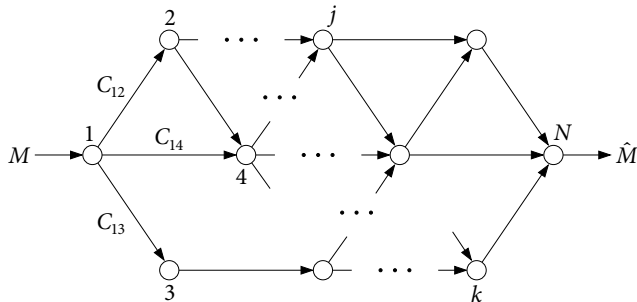
- Canonical problems in network communication
 - ▶ Interference management
 - ▶ Multiple unicast
 - ▶ Wireless relaying
- Solutions from network information theory
- Challenges for the future

Graphical unicast networks



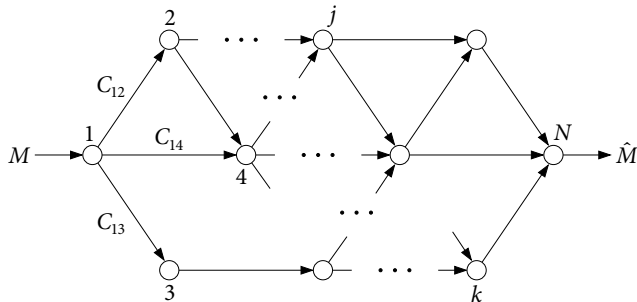
- Model for **wired** networks (Internet, distributed storage, ...)

Graphical unicast networks



- Model for **wired** networks (Internet, distributed storage, ...)
- Directed weighted graph $(\mathcal{N}, \mathcal{E})$ with link capacities C_{jk}

Graphical unicast networks

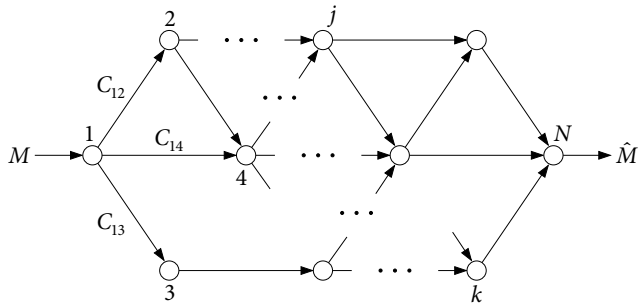


- Model for **wired** networks (Internet, distributed storage, ...)
- Directed weighted graph $(\mathcal{N}, \mathcal{E})$ with link capacities C_{jk}

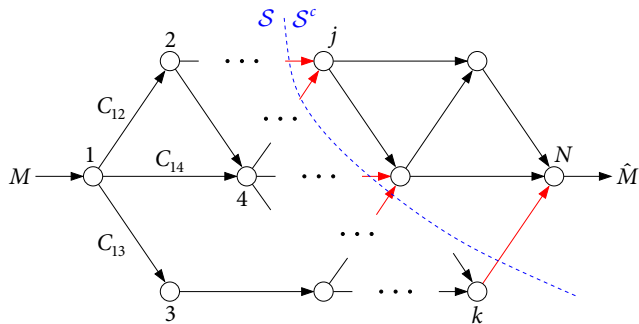
Network information flow questions

- Network capacity
- Optimal coding schemes/protocols/architectures

Max-flow min-cut theorem



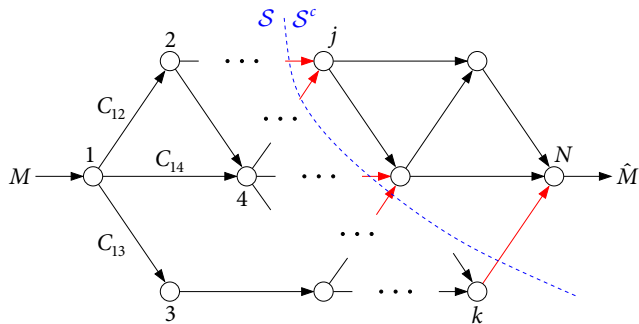
Max-flow min-cut theorem



Ford–Fulkerson (1956)

$$C = \min_{S \subset N: 1 \in S, N \in S^c} C(S)$$

Max-flow min-cut theorem

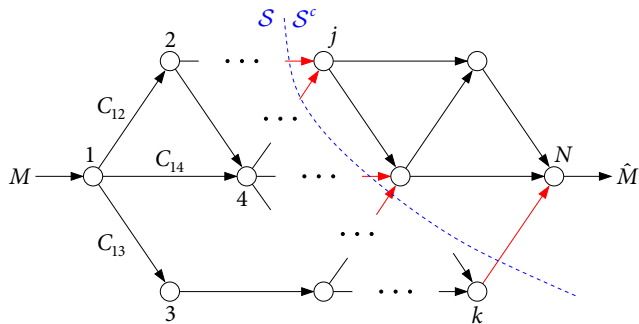


Ford–Fulkerson (1956)

$$C = \min_{S \subset N: 1 \in S, N \in S^c} C(S)$$

- Achieved **error-free** using simple **routing** (Ford–Fulkerson algorithm)

Max-flow min-cut theorem

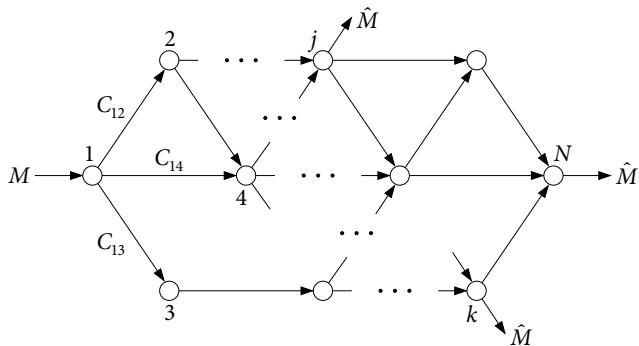


Ford–Fulkerson (1956)

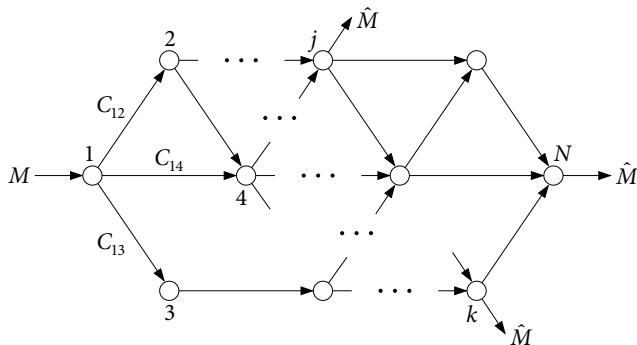
$$C = \min_{S \subset \mathcal{N}: 1 \in S, N \in S^c} C(S)$$

- Achieved **error-free** using simple **routing** (Ford–Fulkerson algorithm)
- Information treated as commodity flow

Graphical **multicast** network



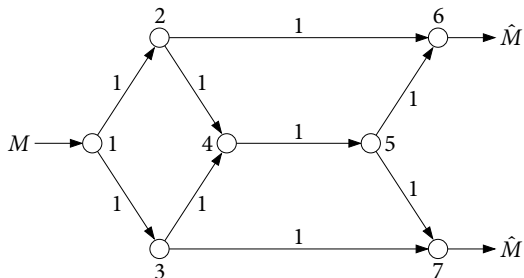
Graphical **multicast** network



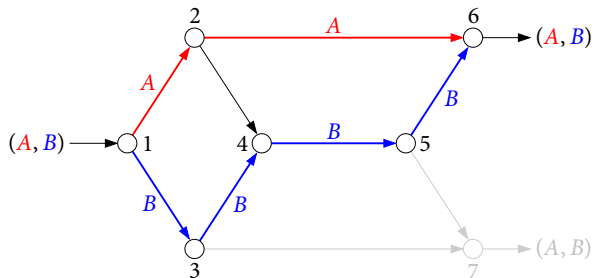
Network information flow questions

- Network capacity?
- Is routing sufficient?

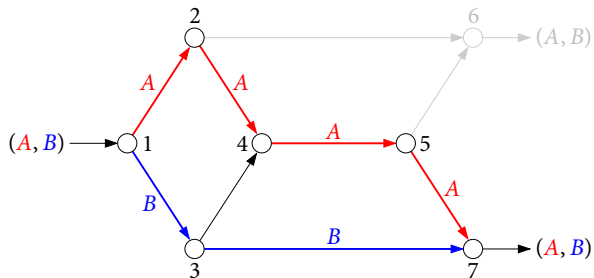
Butterfly network



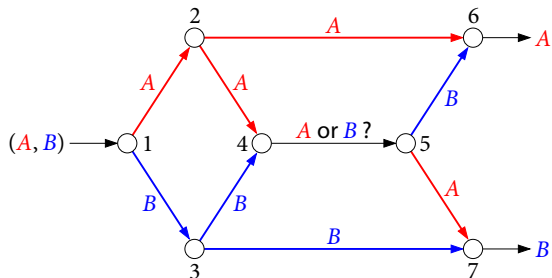
Butterfly network



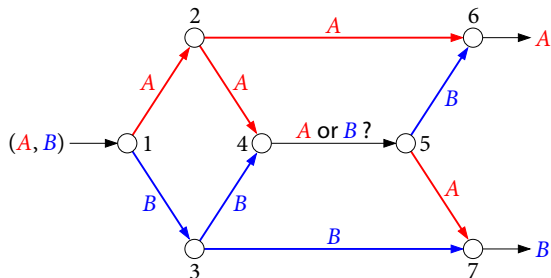
Butterfly network



Butterfly network

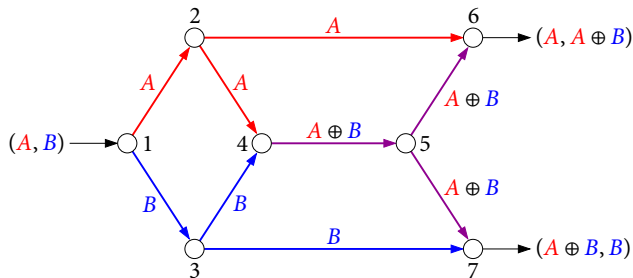


Butterfly network



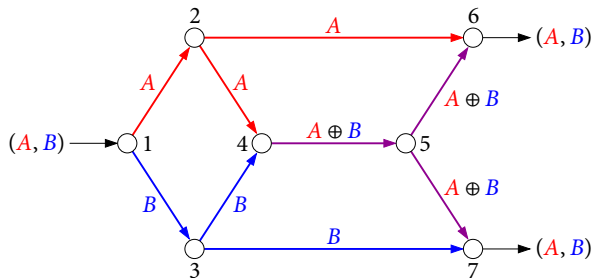
- Routing: $R = 1$

Butterfly network



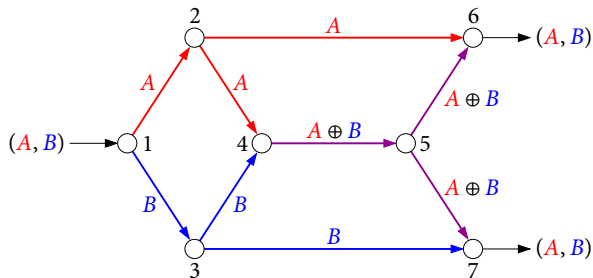
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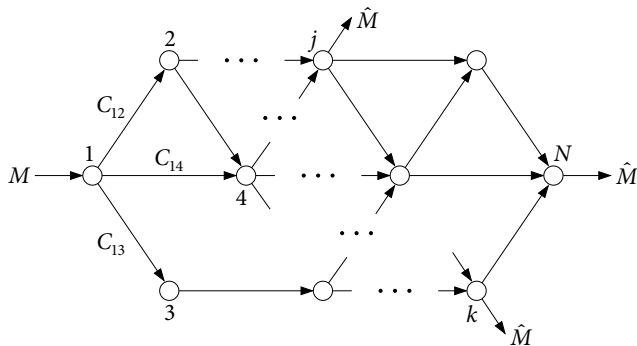
- Routing: $R = 1$
- Coding: $R = 2$ (capacity)

Butterfly network



- Routing: $R = 1$
- Coding: $R = 2$ (capacity)
- Treating information as a commodity is not optimal in general

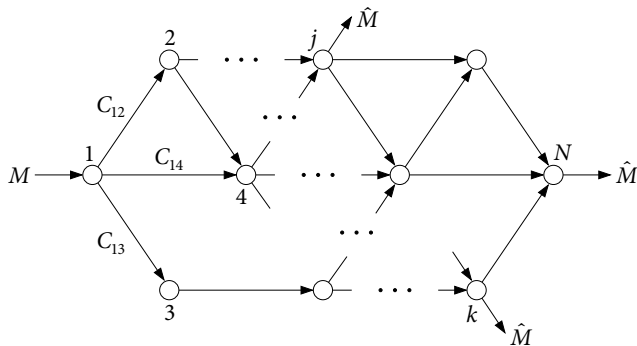
Network coding theorem



Ahlswede–Cai–Li–Yeung (2000)

$$C = \min_{j \in \mathcal{D}} \min_{\substack{S \subset \mathcal{N} \\ 1 \in S, j \in S^c}} C(S)$$

Network coding theorem

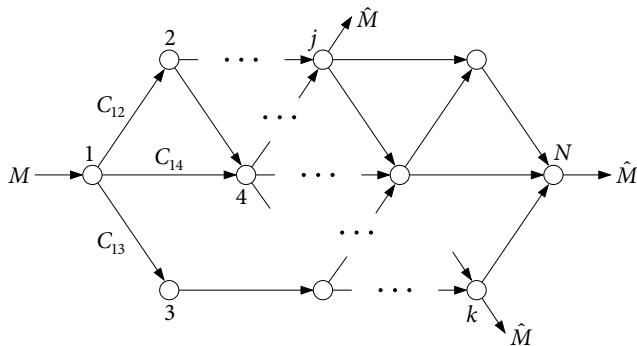


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- Achieved by **linear network coding** (Li–Yeung–Cai 2003, Koetter–Médard 2003)

Network coding theorem

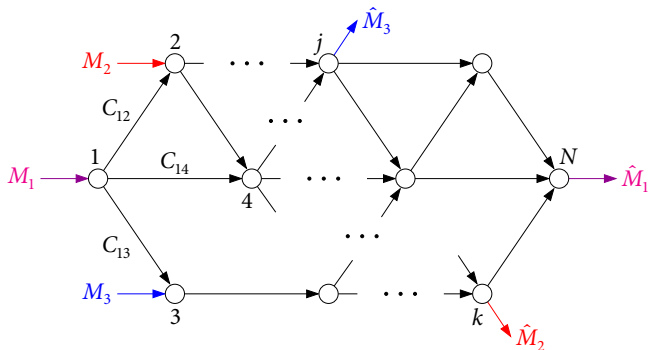


Ahlswede–Cai–Li–Yeung (2000)

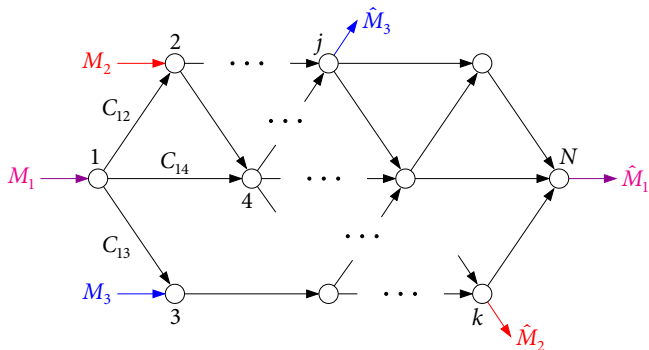
$$C = \min_{j \in \mathcal{D}} \min_{\substack{\mathcal{S} \subseteq \mathcal{N} \\ 1 \in \mathcal{S}, j \in \mathcal{S}^c}} C(\mathcal{S})$$

- Achieved by **linear network coding** (Li–Yeung–Cai 2003, Koetter–Médard 2003)
- **Coded TCP**: performance improvement for wi-fi and cellular networks

Graphical **multiple unicast** network

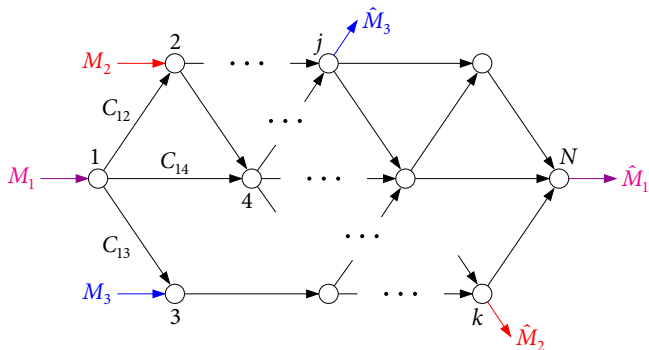


Graphical **multiple unicast** network



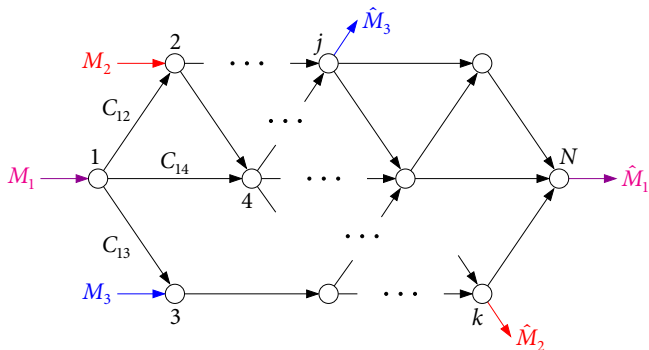
- Capacity **not** known in general even for two flows

Graphical **multiple unicast** network



- Capacity **not** known in general even for two flows
- **Nonlinear network coding** > **linear network coding** > **routing**

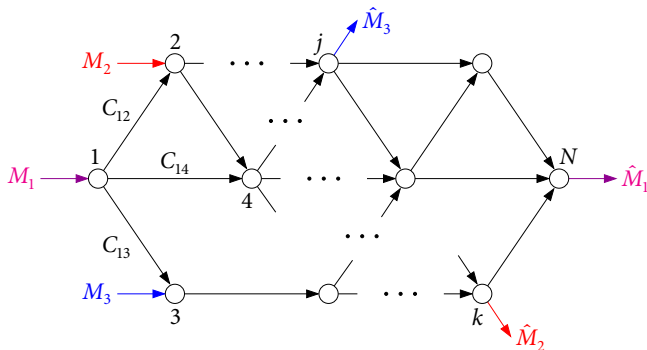
Graphical **multiple unicast** network



Conclusion 2

Coding brings a new dimension to networking

Graphical **multiple unicast** network



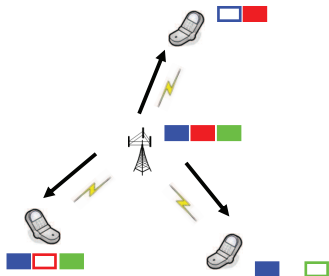
Conclusion 2

Coding brings a new dimension to networking

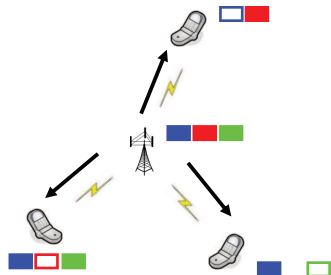
Challenge 2

Network capacity and optimal network coding

Index coding

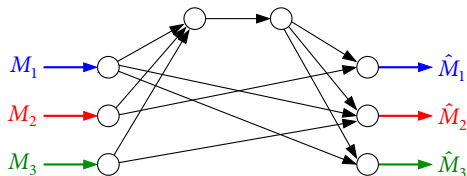
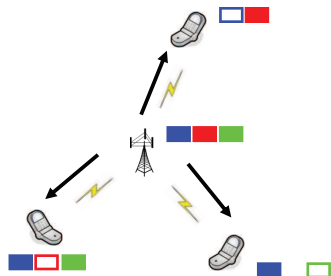


Index coding



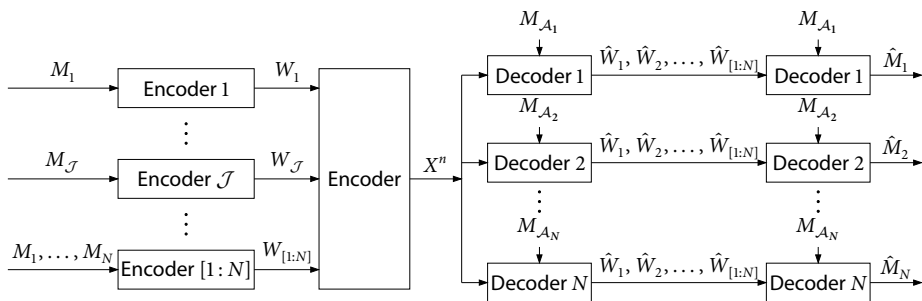
- Content distribution, satellite communication, opportunistic routing, ...
- How many transmissions are needed?
- Which coding minimizes the number of transmissions?

Index coding

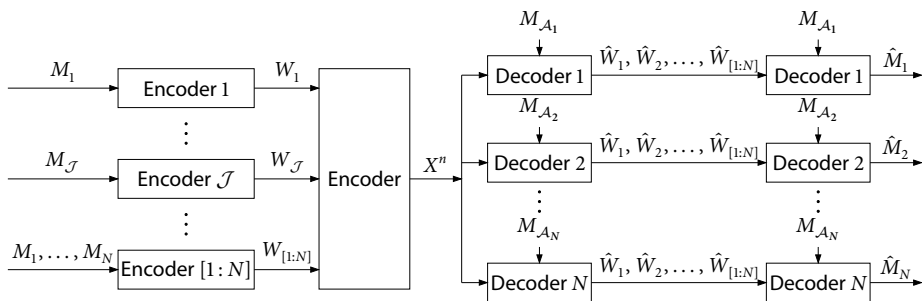


- Content distribution, satellite communication, opportunistic routing, ...
- How many transmissions are needed?
- Which coding minimizes the number of transmissions?
- **Canonical** network coding problem (**broadcast** and **interference**)

Composite coding

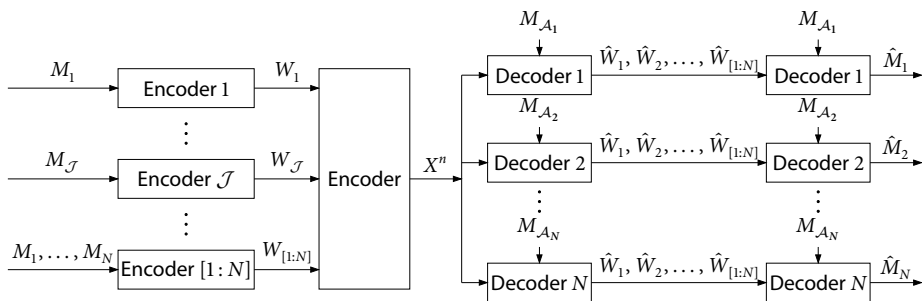


Composite coding



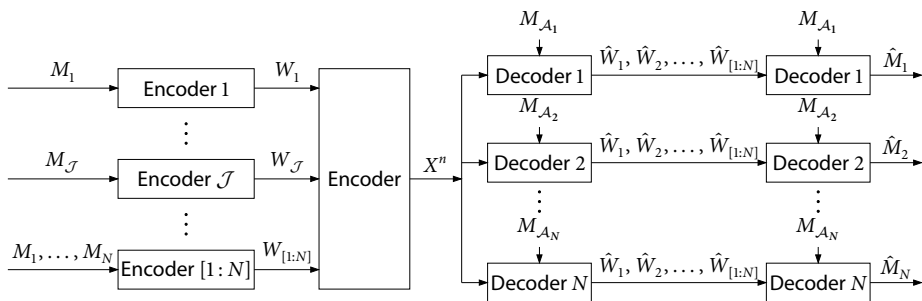
- All 218 index coding problems with $N = 4$

Composite coding



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Composite coding

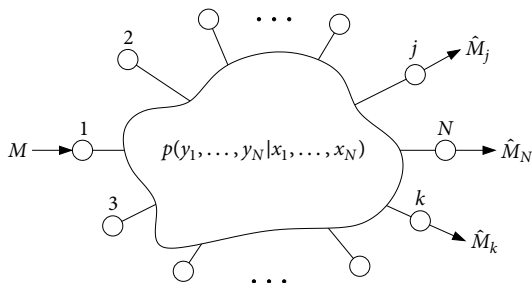


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Outline of the talk

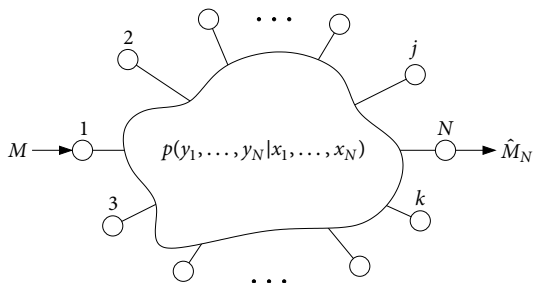
- Canonical problems in network communication
 - ▶ Interference management
 - ▶ Multiple unicast
 - ▶ Wireless relaying
- Solutions from network information theory
- Challenges for the future

Relay network



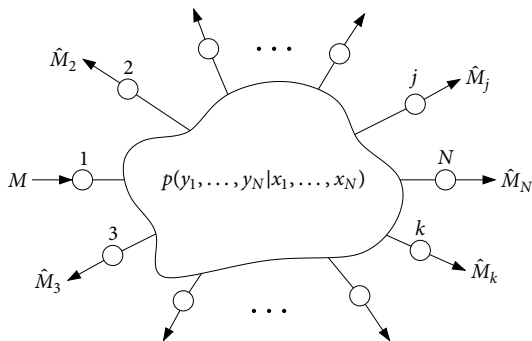
- Nodes: $(X_1, Y_1), \dots, (X_N, Y_N)$
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Relay network



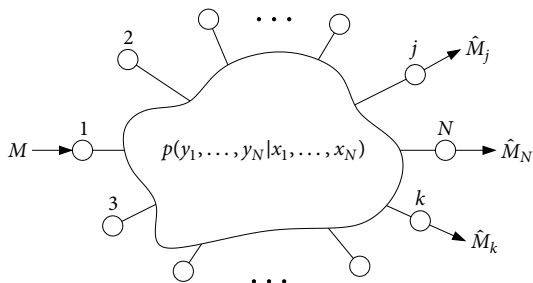
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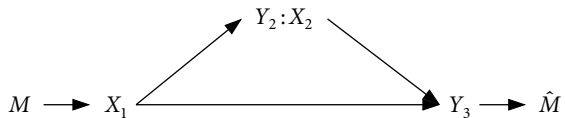
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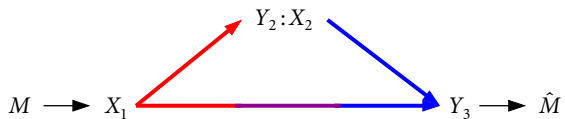
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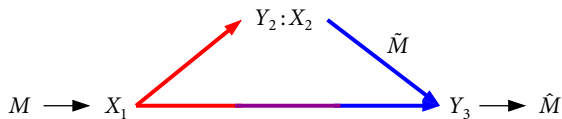
Canonical coding schemes for relay channels



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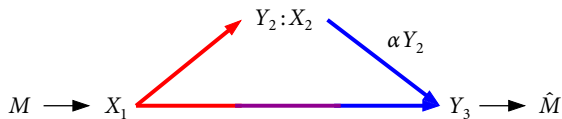


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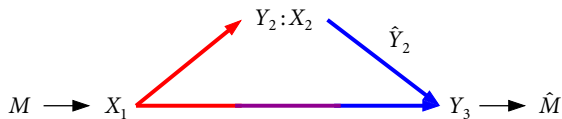
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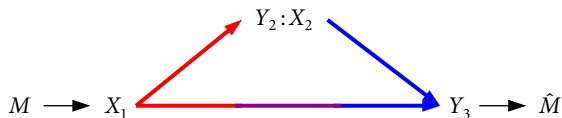
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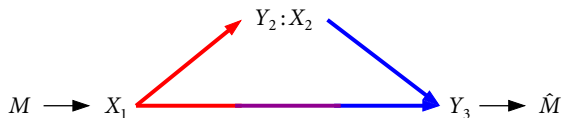
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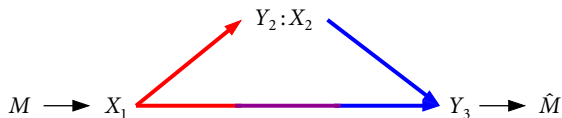


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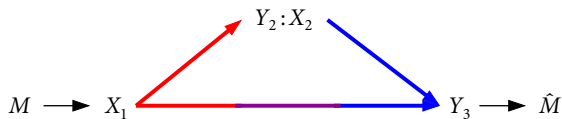
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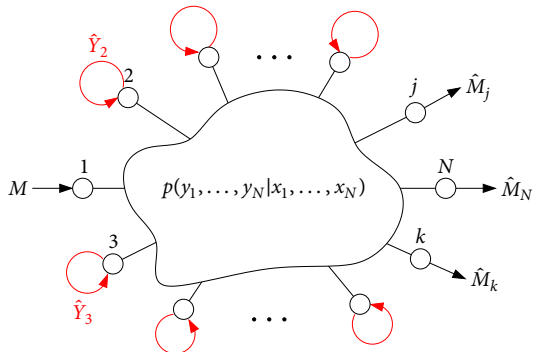
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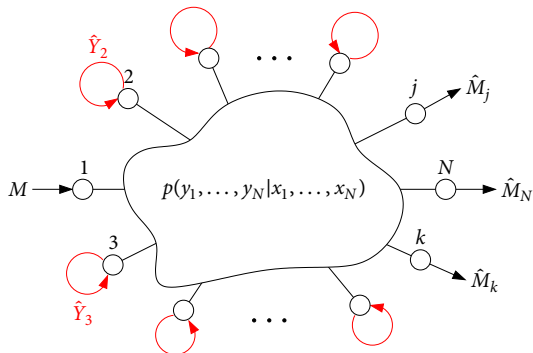
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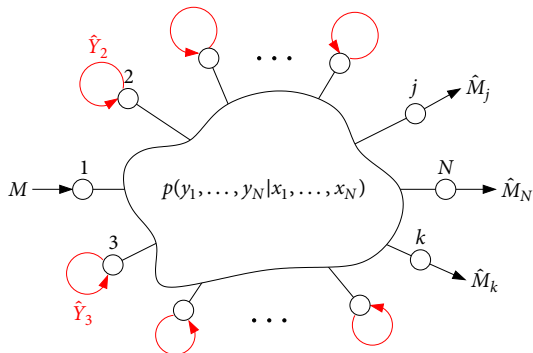
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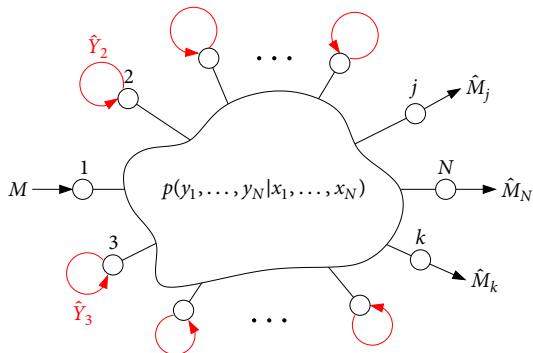
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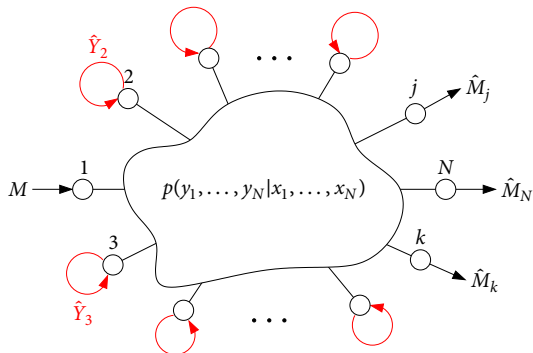
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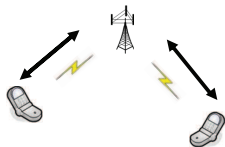
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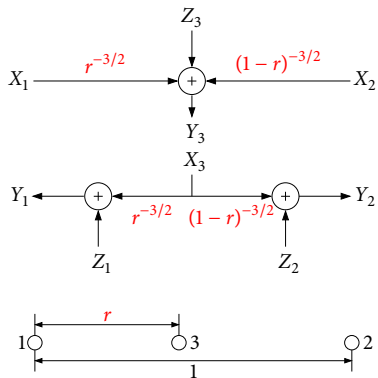


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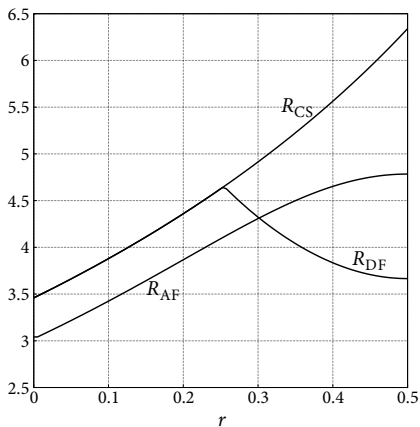
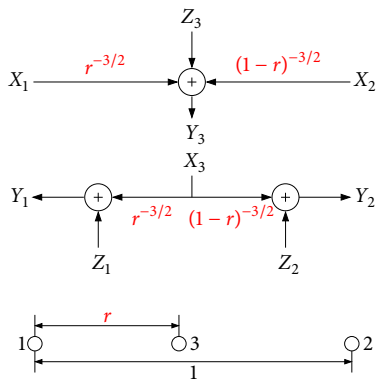
Two-way relay communication



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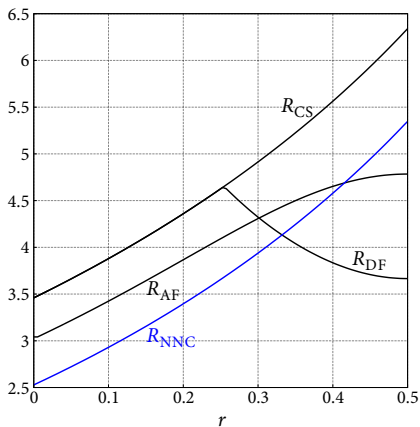
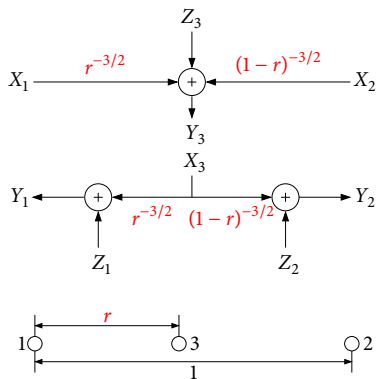


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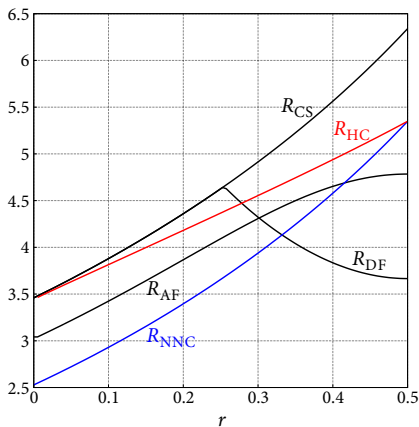
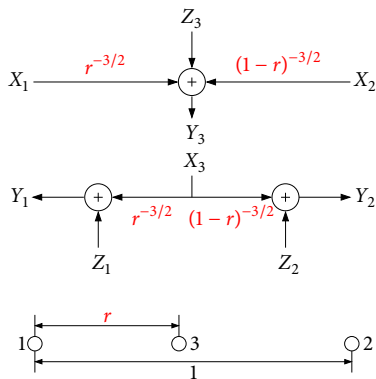
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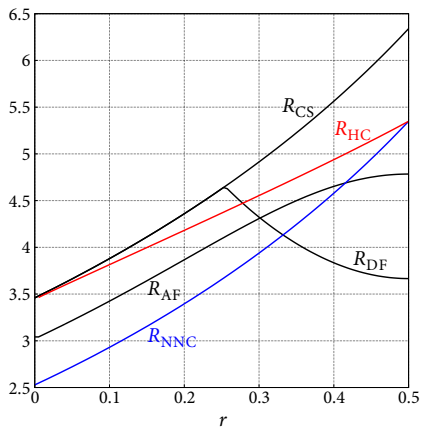
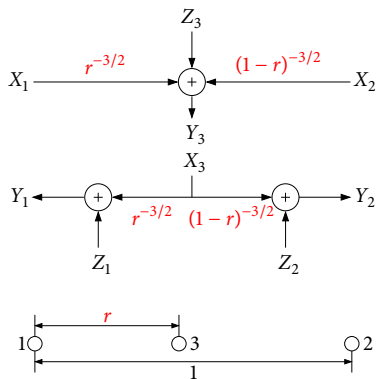
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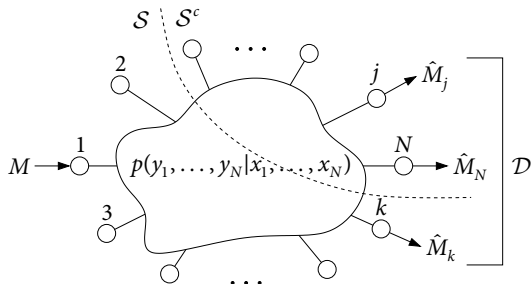
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Conclusion 3

Advanced relaying schemes can outperform traditional schemes

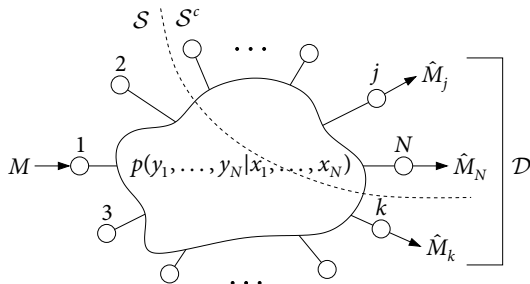
More on noisy network coding



Cutset bound (El Gamal 1981)

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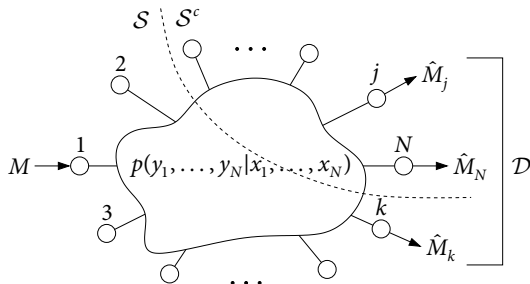
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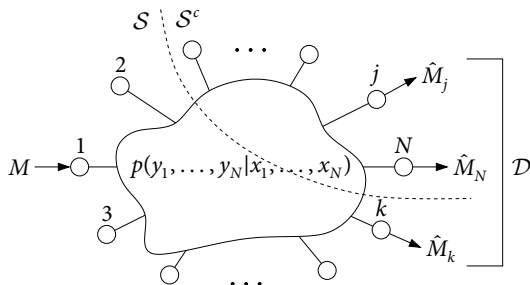
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Noisy network coding bound (Lim–K–El Gamal–Chung 2011)

$$C \geq \max_{k \in \mathcal{D}} \min_{S: 1 \in S, k \in S^c} (I(X(S); \hat{Y}(S^c), Y_k | X(S^c)) - I(Y(S); \hat{Y}(S) | X^N, \hat{Y}(S^c), Y_k)),$$

where the maximum is over all $\prod_{k=1}^N p(x_k) p(\hat{y}_k | y_k, x_k)$

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